

EXAMPLE 8.8 & Exercise 8.76 (Determine pressure drop)

Assume a car's exhaust system can be approximated as 4 m of 0.05-m-diameter cast iron pipe with equivalent of six 90° elbows and a muffler. The muffler acts as a resistor with a loss coefficient of $K_L = 8.5$. Determine the pressure at the beginning of the exhaust system if the flowrate is $3.0 \times 10^{-3} \text{ m}^3/\text{s}$, the temperature is 120°C , and the exhaust has the same properties as air. $\mu = 2.25 \times 10^{-5} \text{ N} \cdot \text{s}/\text{m}^2$

The energy equation is

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + \left(f \frac{\ell}{D} + \sum K_L\right) \frac{V^2}{2g} \quad (1)$$

其中， $z_1 = z_2$ 、 $p_2 = 0$ 且 $V_1 = V_2 = \frac{Q}{A} = \frac{3 \times 10^{-3} \text{ m}^3/\text{sec}}{\pi(0.05\text{m})^2/4} = 1.528 \text{ m/s}$ (2)

將 (2) 代入 (1) $\rightarrow P_1 = \left(f \frac{\ell}{D} + \sum K_L\right) \frac{\rho V^2}{2}$ (3)

其中， $\rho = \frac{P}{RT} = \frac{101.3 \times 10^3 \text{ N}/\text{m}^2}{(286.7 \text{ N} \cdot \text{m}/\text{kg} \cdot \text{K})(273 + 120) \text{ K}} = 0.899 \text{ kg}/\text{m}^3$

由於 $\frac{\varepsilon}{D} = \frac{2.6 \times 10^{-4} \text{ m}}{0.05 \text{ m}} = 0.0052$ 且 $Re = \frac{\rho V D}{\mu} = \frac{(0.899 \text{ kg}/\text{m}^3)(1.528 \text{ m/s})(0.05 \text{ m})}{2.25 \times 10^{-5} \text{ N} \cdot \text{s}/\text{m}^2} = 3,053$

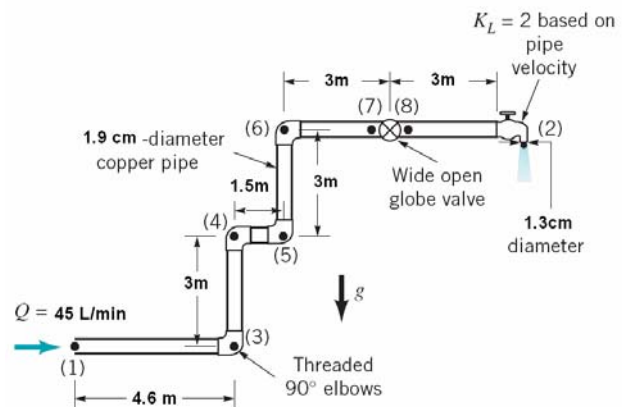
由 Moody chart 查得 $f = 0.047$

代入 (3)

$$P_1 = \left(f \frac{\ell}{D} + \sum K_L\right) \frac{\rho V^2}{2} = \left[0.047 \frac{4 \text{ m}}{0.05 \text{ m}} + 6(0.3) + 8.5\right] \frac{1}{2} (0.899 \text{ kg}/\text{m}^3)(1.528 \text{ m/s})^2 = 14.756 \text{ N}/\text{m}^2$$

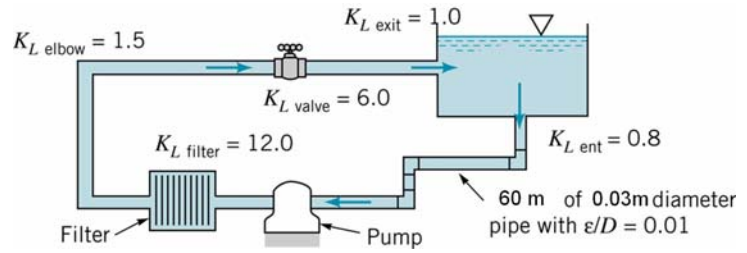
EXAMPLE 8.8 (Determine pressure drop)

Water at 15°C flows from the basement to the second floor through the 1.9 cm-diameter copper pipe (a drawn tubing) at a rate of $Q = 45 \text{ L}/\text{min} = 7.5 \times 10^{-4} \text{ m}^3/\text{s}$ and exits through a faucet of diameter 1.3 cm as shown. Determine the pressure at point (1) if: (a) all losses are neglected, (b) the only losses included are major losses, or (c) all losses are included.



EXAMPLE 8.11 & Exercise 8.99 (Determine flowrate)

Water is circulated from a large tank, through a filter, and back to the tank as shown. The power added to the water by the pump is 270 N·m/s. Determine the flowrate through the filter.



The energy equation is

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 + h_p = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + \left(f \frac{\ell}{D} + \sum K_L\right) \frac{V^2}{2g} \quad (1)$$

其中， $z_1 = z_2$ 、 $p_1 = p_2$ 、 $V_1 = V_2 = 0$ 且

$$h_p = \frac{\dot{W}_p}{\gamma Q} = \frac{270 \text{ N} \cdot \text{m/s}}{9800 \frac{\text{N}}{\text{m}^3} \left(\frac{\pi}{4} (0.03 \text{ m})^2\right) V} = \frac{38.977}{V} \quad (2)$$

$$\text{將 (2) 代入 (1)} \rightarrow \frac{39}{V} = \left(f \frac{60 \text{ m}}{0.03 \text{ m}} + 5(1.5) + 12 + 6 + 1\right) \frac{V^2}{2(9.81 \text{ m/s}^2)} \rightarrow$$

$$V^3 = \frac{0.383}{f + 0.01365} \quad (3)$$

$$\text{加上 } Re = \frac{\rho V D}{\mu} = \frac{10^3 \text{ kg/m}^3 V \text{ m/s} (0.03 \text{ m})}{1.12 \times 10^{-3} \text{ N} \cdot \text{s/m}^2} = 26,785.714 V \quad (4)$$

透過 trial and error scheme... (請詳列過程)

◎先假設 $f = 0.04$ → 代入 (3) 得到 $V = 1.93 \text{ m/s}$ ；代入 (4) 得到 $Re = 5.17 \times 10^4$ →

利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.039$ (一猜就差不遠) → 再確認。

◎再假設 $f = 0.039$ → 代入 (3) 得到 $V = 1.94 \text{ m/s}$ ；代入 (4) 得到 $Re = 5.19 \times 10^4$ →

利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.039$ (可)。

Flowrate $Q = AV = \dots$

EXAMPLE 8.13 & Exercise 8.100 (Determine diameter)

A certain process requires $6.25 \times 10^{-2} \text{ m}^3/\text{s}$ of water to be delivered a pressure of 205 kPa. This water comes from a large diameter supply main in which the pressure remains at 415 kPa. If the galvanized iron pipe connecting the two locations is 60 m long and contains six threaded 90° elbows, determine the pipe diameter. Elevation differences are negligible.

The loss coefficient $K_L = 1.5$ for each elbow and $K_L = 0.5$ for the entrance.

$$\nu = 1.12 \times 10^{-6} \text{ m}^2/\text{s} \quad \varepsilon = 0.15 \text{ mm}$$

The energy equation is

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2 + \left(f \frac{\ell}{D} + \sum K_L\right) \frac{V^2}{2g} \quad (1)$$

其中， $z_1 = z_2$ 、 $p_1 = 415 \text{ kPa}$ 、 $p_2 = 205 \text{ kPa}$ 且

$$V_1 = 0, \quad V_2 = \frac{Q}{A} = \frac{6.25 \times 10^{-2} \text{ m}^3/\text{sec}}{\pi D^2/4} = \frac{0.08}{D^2} \text{ m/s} \quad (2)$$

將 (2) 代入 (1) $\rightarrow P_1 - P_2 = \left(f \frac{\ell}{D} + \sum K_L\right) \frac{\rho V^2}{2} \rightarrow$

$$(415 - 205) \times 10^3 \text{ N/m}^2 = \left(1 + f \frac{60 \text{ m}}{D} + 6(1.5) + 0.5\right) \frac{10^3 \text{ kg/m}^3}{2} \left(\frac{0.08}{D^2}\right)^2 \rightarrow$$

$$6250 = \left(1 + \frac{5.7f}{D}\right) \frac{1}{D^4} \quad (3)$$

$$\text{加上 } \frac{\varepsilon}{D} = \frac{0.15 \text{ mm}}{D} \quad (4) \quad \text{且 } \text{Re} = \frac{VD}{\nu} = \frac{(0.08/D^2)D}{1.12 \times 10^{-6} \text{ m}^2/\text{s}} = \frac{7.14 \times 10^4}{D} \quad (5)$$

透過 trial and error scheme... (請詳列過程)

- ◎先假設 $D = 0.12 \text{ m}$ \rightarrow 代入 (3) 得到 $f = 6.23 \times 10^{-3}$ ；代入 (4) 得到 $\varepsilon/D = 0.00125$ ；代入 (5) 得到 $\text{Re} = 5.95 \times 10^5 \rightarrow$ 利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.021 \neq 6.23 \times 10^{-3}$ (誤差 10% 以上) \rightarrow 再假設不同的 D 值
- ◎再假設 $D = 0.15 \text{ m}$ \rightarrow 代入 (3) 得到 $f = 0.026$ ；代入 (4) 得到 $\varepsilon/D = 0.001$ ；代入 (5) 得到 $\text{Re} = 4.76 \times 10^5 \rightarrow$ 利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.0203 \neq 0.026$ (誤差 10% 以上) \rightarrow 再假設不同的 D 值
- ◎再假設 $D = 0.14 \text{ m}$ \rightarrow 代入 (3) 得到 $f = 0.034$ ；代入 (4) 得到 $\varepsilon/D = 0.00111$ ；代入 (5) 得到 $\text{Re} = 5.1 \times 10^5 \rightarrow$ 利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.0205 \neq 0.034$ (誤差 10% 以上) \rightarrow 再假設不同的 D 值
- ◎再假設 $D = 0.13 \text{ m}$ \rightarrow 代入 (3) 得到 $f = 0.023$ ；代入 (4) 得到 $\varepsilon/D = 0.00115$ ；代入 (5) 得到 $\text{Re} = 5.5 \times 10^5 \rightarrow$ 利用 ε/D 與 Re 查詢 Moody chart 得知 $f = 0.0205 \neq 0.023$ (誤差 10% 以上) \rightarrow 再假設不同的 D 值
- ◎再假設 $D = 0.135 \text{ m} \dots$